



Syntax-Guided Synthesis of Datalog Programs

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ABSTRACT

Datalog has witnessed promising applications in a variety of domains. We propose a programming-by-example system, ALPS, to synthesize Datalog programs from input-output examples. Scaling synthesis to realistic programs in this manner is challenging due to the rich expressivity of Datalog. We present a *syntax-guided* synthesis approach that prunes the search space by exploiting the observation that in practice Datalog programs comprise rules that have similar latent syntactic structure. We evaluate ALPS on a suite of 34 benchmarks from three domains—knowledge discovery, program analysis, and database queries. The evaluation shows that ALPS can synthesize 33 of these benchmarks, and outperforms the state-of-the-art tools Metagol and Zaatar, which can synthesize only up to 10 of the benchmarks.

CCS CONCEPTS

• **Theory of computation** → **Program analysis**; **Active learning**; • **Software and its engineering** → **Programming by example**; **Domain specific languages**; • **Information systems** → **Relational database query languages**;

KEYWORDS

Syntax-guided synthesis, Datalog, Active learning, Template augmentation, Program analysis

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1 INTRODUCTION

Datalog, a declarative logic programming language, has witnessed promising applications in a variety of domains, including bioinformatics [33, 58], big-data analytics [30, 60, 63], natural language processing [44], networking [39], program analysis [17, 26], and robotics [56]. A key reason is the emergence of scalable Datalog solvers, including open-source [1, 3, 11, 59, 60] and commercial ones [2, 4, 6, 25]. Moreover, the concise and declarative nature of Datalog has made it the target of a growing body of meta-reasoning tools. For instance, program analyses written in Datalog are readily extensible with features such as fixed point frameworks [14, 40], abstraction refinement [74], and user interaction [41, 57, 73]. Likewise, software-defined networking (SDN) applications written in Datalog can avail of efficient provenance tracking to help in tasks such as debugging and repairing [71].

A key hindrance to bringing these benefits to a broad user base is the lack of automated tools to help develop Datalog programs. To this end, we propose a programming-by-example system, ALPS, to synthesize Datalog programs from input-output examples. This constitutes a natural next step in many domains such as program analysis and networking, where reference imperative implementations can provide input-output examples.

While ostensibly simple, synthesizing such programs is challenging because Datalog is powerful enough to capture all polynomial time computations. Learning logic programs from examples has been extensively studied in a subfield of machine learning called *inductive logic programming* (ILP) [45, 49]. However, even state-of-the-art ILP techniques are very limited in their ability to learn realistic Datalog programs [9, 50].

We propose a new approach to synthesize Datalog programs. Our key insight is that such programs in practice comprise rules that have similar latent syntactic structure. Our approach exploits this insight via the *syntax-guided program synthesis* paradigm [10], wherein the syntactic structure of the target class of programs is leveraged to efficiently traverse the hypothesis space of programs. For this purpose, our approach must address three key challenges: (i) capture syntactic structure effectively, (ii) minimize the number of examples needed, and (iii) explore the search space efficiently. We next elaborate upon each of these objectives.

To capture the syntactic structure of rule-based programs, we use *meta-rules* [50]—templates that describe a set of possible rules that can appear in a program. The key challenge is to obtain a set of meta-rules that is *general enough to capture useful programs*

but specific enough to enable efficient synthesis. We propose a novel approach to systematically generate meta-rules, taking advantage of domain knowledge.

To minimize the number of examples needed, our approach aims to ask an oracle a small number of queries concerning the expected output on a given input. The oracle need only answer with *yes* or *no*, rather than crafting elaborate examples and supplying them to the synthesizer. We use an *active learning* technique, called *query by committee* (QBC) [24, 62], to pick an example that can prune the search space the most. In our setting, QBC takes as input a committee formed by a set of consistent programs, and returns an example on which the committee *disagrees the most*—the most controversial example. We then prune the programs that disagree with the given label and repeat the process. However, it is infeasible to apply QBC on the entire search space, which is prohibitively large.

To explore the search space efficiently and overcome the challenge in using QBC, we use a *bidirectional synthesis strategy* to maintain the *most-general* and *most-specific* programs that are consistent with the given examples [43]. Intuitively, the most-general and most-specific programs (defined through logical entailment) form a representative set of the search space, allowing us to preserve exactness of the search. Moreover, this set is much smaller than the size of the search space, making it an ideal *committee*. To incrementally update the search space as examples are labeled, we define efficient *top-down* and *bottom-up refinement operators* that are guided by the given set of meta-rules.

We have implemented our end-to-end approach in the ALPS system and report on our experience evaluating it on a diverse set of 34 benchmarks from three domains: knowledge discovery, program analysis, and relational queries. The evaluation shows that ALPS can synthesize 33 of these benchmarks, and outperforms the state-of-the-art tools Metagol [19] and Zaatar [9], which can synthesize only up to 10 of the benchmarks.

We summarize the main contributions of this paper:

- We present a syntax-guided approach and system ALPS for synthesizing Datalog programs from input-output examples.
- ALPS employs a bidirectional search strategy to efficiently traverse the space of possible programs.
- ALPS minimizes the number of required examples using an active learning technique called query-by-committee.
- We demonstrate the effectiveness of ALPS at synthesizing realistic Datalog programs from diverse domains and its ability to outperform existing state-of-the-art techniques.

2 OVERVIEW EXAMPLES

ALPS learns Datalog programs that are correct with respect to a given instance of input and output relations. In this section, we first present two illustrative examples that highlight applications of ALPS in two domains: program analysis and relational queries. We then present an example to elucidate key design choices in ALPS. We also use it as the running example in the rest of the paper.

Example 2.1 (Program analysis). Datalog has shown great potential in the domain of program analysis [22, 40, 51, 59, 65]. Thus, there is a growing need to help synthesize program analyzers in Datalog for a variety of programming languages, including general-purpose and domain-specific ones.

We demonstrate how ALPS can be used to learn a static analysis to detect API misuses—a common source of bugs in today’s world of complex and evolving APIs. For a given example program with known API misuses, we populate input relations representing the syntax of the program and output relations representing the bugs. Then, ALPS learns Datalog rules that can be used for detecting similar API misuses.

Consider the following C program using the OpenSSL API. Functions `ssl_socket_open1-4` establish a SSL socket and return a constant `OK` if they succeed. Two functions `ssl_socket_open{2,4}` contain API misuses in that they incorrectly return `OK` when a SSL socket is not properly established.

```

1  int ssl_socket_open1(SSL* ssl) {
2      X509* cert = SSL_get_peer_certificate(ssl);
3      long err = SSL_get_verify_result(ssl);
4      if (!cert) {...}
5      if (err == X509_V_OK) { ... }
6      return OK; // correct
7  }
8
9  int ssl_socket_open2(SSL* ssl) {
10     X509* cert = SSL_get_peer_certificate(ssl);
11     if (cert == NULL) {...}
12     long err = SSL_get_verify_result(ssl);
13     ...
14     return OK; // incorrect (missing check on err)
15 }
16
17 int ssl_socket_open3(SSL* ssl) {
18     long err = SSL_get_verify_result(ssl);
19     if (err != X509_V_OK) {...}
20     X509* cert = SSL_get_peer_certificate(ssl);
21     if (cert) {...}
22     return OK; // correct
23 }
24
25 int ssl_socket_open4(SSL* ssl) {
26     long err = SSL_get_verify_result(ssl);
27     switch (err) {
28         case X509_V_OK:
29             cert = SSL_get_peer_certificate(ssl);
30         }
31     return OK; // incorrect (missing check on cert)
32 }

```

Our goal is to learn a Datalog program that detects functions that misuse the OpenSSL API, whose behavior is defined as follows:

- `SSL_get_peer_certificate` returns a pointer to the X509 certificate the peer presented. If the peer did not present a certificate, `NULL` is returned.
- `SSL_get_verify_result` returns the result of the verification of the X509 certificate presented by the peer, if any. It returns a constant named `X509_V_OK` if the verification succeeded or if no peer certificate was presented.

Functions should return `OK` only if (i) `SSL_get_peer_certificate` returns a non-null pointer, and (ii) `SSL_get_verify_result` returns the constant named `X509_V_OK`.

The problem involves four input relations and one output relation with the following meaning:

- $\text{OpSucc}(l1, l2)$: Program control may flow from line $l1$ to $l2$.
- $\text{Check}(x, l)$: The value of variable x is compared to a specific value at line l .
- $\text{Certify}(x, l)$: Variable x at line l is assigned the return value of `SSL_get_peer_certificate()`.
- $\text{Verify}(x, l)$: Variable x at line l is assigned the return value of `SSL_get_verify_result()`.
- $\text{Ok}(l)$: The function that returns OK at line l correctly uses the OpenSSL API.

Relations OpSucc and Check are pre-defined as part of the program's intermediate representation while relations Certify and Verify can be automatically extracted from a given API, in this case OpenSSL. We provide an instance of these relations encoding the analyzed C program to ALPS, namely

```
Certify(cert,2), Verify(err,3), Check(cert,4), Check(err,5), ...
```

along with $\text{Ok}(6)$ and $\text{Ok}(22)$ as positive examples and $\text{Ok}(14)$ and $\text{Ok}(31)$ as negative examples in the output relation. ALPS generates the following program in 6 minutes.

```
CertFlow(x,l2) :- Certify(x,l1), OpSucc(l1,l2).
VeriFlow(x,l2) :- Verify(x,l1), OpSucc(l1,l2).
CertCheck(l2) :- CertFlow(x,l1), Check(x,l1), OpSucc(l1,l2).
VeriCheck(l2) :- VeriFlow(x,l1), Check(x,l1), OpSucc(l1,l2).
Ok(l) :- CertCheck(l), VeriCheck(l).
```

The rules are intended to be read right-to-left, with all variables universally quantified, and the $:-$ operator interpreted as implication. Note that predicates $\text{CertFlow}(x, l)$, $\text{VeriFlow}(x, l)$, $\text{CertCheck}(l)$, and $\text{VeriCheck}(l)$ are not specified among the input or output relations; they are invented by ALPS, highlighting the rich space of programs it explores.¹ We elaborate on how the search space is determined in Section 4.1. The relation $\text{CertFlow}(x, l)$ ($\text{VeriFlow}(x, l)$ resp.) indicates the return value of `SSL_get_peer_certificate` (`SSL_get_verify_result` resp.) flows to line l . The relation $\text{CertCheck}(l)$ ($\text{VeriCheck}(l)$ resp.) means the return value of `SSL_get_peer_certificate` (`SSL_get_verify_result` resp.) is compared to a specific value and control flows to line l .

The Datalog program correctly captures an important portion of the proper use of the OpenSSL API. This example illustrates that ALPS represents a promising step towards synthesizing usable program analyzers. On the contrary, the state-of-the-art ILP tools Metagol and Zaatar fail to synthesize the program within 3 hours.

Example 2.2 (Relational queries). Datalog is widely used as a relational query language due to its expressiveness and scalable performance [13, 27, 59]. ALPS can be used to synthesize sophisticated relational queries in Datalog from input-output behaviors.

We illustrate using ALPS to synthesize a relational query for finding students who take two different classes on the same day. The problem involves three input relations and one output relation with the following meaning:

- $\text{Student}(s, n)$: Student s is associated with the ID n .
- $\text{Class}(c, d)$: Class c is held on day d .
- $\text{Enrolled}(n, c)$: The student having ID n is enrolled in class c .
- $\text{Busy}(s)$: Student s takes two different classes on the same day.

¹For readability, we provide intuitive names for invented predicates instead of mechanically generated ones by ALPS.

It is natural in a programming-by-example setting for the user to provide an instance specifying the input-output behavior of the desired query. Using such an instance comprising input relations regarding 14 students and 6 classes, and 5 examples in the output relation `Busy`, ALPS synthesizes the following Datalog program within 18 seconds:

```
EnrollClass(n, c, l) :- Enrolled(n, c), Class(c, l).
Busy(s) :- Student(s, n), EnrollClass(n, c1, l), EnrollClass(n, c2, l),
         c1 != c2.
```

where `EnrollClass` is an invented predicate. While ostensibly simple, the above query is non-trivial to synthesize since it is semantically equivalent to the following complex SQL query:²

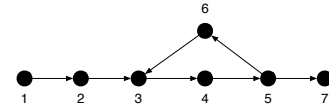
```
SELECT S.s FROM Student S
WHERE S.n IN (SELECT E1.n
              FROM Enrolled E1, Enrolled E2, Class C1, Class C2
              WHERE E1.n = E2.n AND E1.c <> E2.c
              AND E1.c = C1.c AND E2.c = C2.c AND C1.d = C2.d))
```

In contrast, a state-of-the-art tool Scythe [69] for synthesizing SQL queries fails to generate the above SQL query within 3 hours.

Example 2.3 (Knowledge discovery). We demonstrate how ALPS synthesizes a prototypical program in knowledge discovery that is commonly used in the ILP literature: computing the transitive closure of a directed graph. The problem involves one input relation `edge` and one output relation `path` with the following meaning:

- $\text{edge}(x, y)$: there is an edge from node x to node y .
- $\text{path}(x, y)$: there is a path from node x to node y .

Suppose the user populates the input relation, `edge`, with the following example graph:



where an edge from node i to node j indicates that $\text{edge}(i, j)$ appears in the input relation.

Given 4 examples of the output relation `path`, ALPS synthesizes the following recursive program in less than one second, which computes the transitive closure of a directed graph.

```
path(x, y) :- edge(x, y).
path(x, z) :- path(x, y), edge(y, z).
```

In fact, since ALPS maintains all possible programs, it also discovers the following *non-linear* recursive program:

```
path(x, y) :- edge(x, y).
path(x, z) :- path(x, y), path(y, z).
```

We next elaborate on three techniques that ALPS combines synergistically in order to realize this result.

Meta-rule-guided synthesis. Learning Datalog programs is a complex task; even approximate learning is hard [18].³ To overcome this barrier, ALPS exploits the observation that in practice Datalog programs comprise rules with similar latent syntactic structure.

²Datalog can in fact be viewed as augmenting relational algebra, which is widely used in the form of SQL, with recursion.

³In approximate learning, the learnt program is not guaranteed to be consistent with the given examples.

Note that both of the recursive rules above are very similar: the only difference is in the relation names. We capture such similarities via the notion of *meta-rules* [50] which are essentially Horn clauses where the relation names are kept abstract and can be instantiated later. Then both of the recursive rules are instances of the meta-rule:

$$R_0(x, z) :- R_1(x, y), R_2(y, z).$$

Many Datalog rules follow a similar chain pattern. This suggests a strategy for synthesizing Datalog programs: enumerate all possible instantiations of the above meta-rule with concrete relation names and examine their combinations. Furthermore, we can think of slight variations of this pattern to capture a broader range of programs. For example, the first rule in Example 2.2 is a slight variation of this meta-rule, the only difference being the arity of predicate `EnrollClass`. We formalize this concept via a process called *augmentation* (see Section 4.4).

Query-by-Committee (qbc). ALPS uses an active learning technique to iteratively pose membership queries about the contents of the output relation, which can be answered upfront or in an interactive manner. To minimize the number of queries, at each step, ALPS picks a query that can prune the space of candidate programs the most to converge to the oracle’s desired program. In the above example, it begins by posing the query: *Is there a path from 1 to 2?* It obtains the answer *yes*. ALPS then poses the next query: *Is there a path from 3 to 2?* It obtains the answer *no*, and the process continues. After 4 queries out of 49 possible queries—all pairs (i, j) where $i, j \in [1, 7]$, ALPS arrives at the above programs. In contrast, picking examples to query randomly may result in a large number of questions. For instance, in 100 trials with random selection, the maximum number of queries is 27, with an average of 12.

Bidirectional search strategy. To explore the search space efficiently, we propose a bidirectional synthesis strategy to maintain a concise committee, i.e., the most-general and most-specific programs that are consistent with current available examples. In our running example, using this strategy results in only 384 programs being evaluated during the search, out of over 10^4 possible programs in the search space.

The above three techniques are combined in a synergistical manner in ALPS: meta-rules define a reasonably large and rich space of candidate programs; the syntactic structure of the space enables bidirectional search to efficiently represent and effectively refine all consistent candidate programs as a concise committee; and, using this committee, qbc guides the refinement by picking the most controversial example to query in the next iteration.

3 PROBLEM FORMULATION

In this section, we formalize Datalog and the synthesis problem.

3.1 Datalog Programs

Rules. A term t is either a variable x, y, z, \dots , or a constant a, b, c, \dots . A relation symbol p, q, r, \dots is associated with an arity $ar(r)$. An atom is an application of a relation symbol to a vector of variables and constants, e.g., $r(x, y, a)$ for a relation r with arity 3. A ground atom is an application of a relation symbol to constants, e.g., $r(a_1, \dots, a_n)$, where a_i are constants. A Datalog rule C is an expression of the form:

$$A :- B_1, B_2, \dots, B_n.$$

where A, B_1, \dots, B_n are atoms. The atom A is called the *head* of the rule; the set of atoms $\{B_1, \dots, B_n\}$ is called the *body* of the rule. A Datalog rule can be interpreted as a logical implication: if B_1, \dots, B_n are true, then so is A .

Programs. A Datalog program P is a finite set of rules. We divide relation symbols into two categories: the *input relations* whose contents are given, and the *output relations* whose contents are derived from the input relations using the program P . An input relation can never appear in the head of a rule. We use I to denote the set of *facts* (ground atoms) in the input relations. The *Herbrand base* \mathcal{B} denotes all possible applications of the output relations to vectors of constants in I . A Datalog program is *recursive* if a relation symbol appears in both the head and the body of a rule.

Semantically, evaluating P on I yields a *minimal Herbrand model* of $P \cup I$, which is the smallest set of ground atoms that satisfies the rules in P and input I . Given a ground atom e , $P \cup I \models e$ denotes that P with input I derives fact e .

3.2 Synthesis Problem

Our task is to synthesize Datalog programs through examples. An *example* is a ground atom from the Herbrand base \mathcal{B} , which can be labeled as positive (+) or negative (-). We are now ready to define our synthesis problem.

Definition 3.1 (Synthesis problem). A synthesis problem S is a tuple $(\mathcal{H}, \mathcal{O}, I)$, where

- \mathcal{H} is a set of Datalog programs, i.e. the *hypothesis space*;
- \mathcal{O} is an *oracle* that labels each example with $\{+, -\}$;
- I is a set of inputs—facts in the input relations.

Let $E_O^+ = \{e \in \mathcal{B} \mid \mathcal{O}(e) = +\}$ and $E_O^- = \{e \in \mathcal{B} \mid \mathcal{O}(e) = -\}$ be the positive and negative examples defined by the oracle respectively. The goal is to find $P \in \mathcal{H}$ such that: for all $e \in E_O^+$, $P \cup I \models e$, and for all $e \in E_O^-$, $P \cup I \not\models e$.

Given a synthesis problem $(\mathcal{H}, \mathcal{O}, I)$, the set of all Datalog programs $P \in \mathcal{H}$ that are consistent with $E = (E^+, E^-)$ is called the *version space*, and is denoted \mathcal{V}_E .

4 OUR APPROACH

In this section, we present the synthesis algorithm underlying ALPS. Section 4.1 describes the structure of the search space. Section 4.2 presents the algorithm parameterized by refinement operators. Section 4.3 instantiates the algorithm with meta-rules. Section 4.4 describes our methodology for designing meta-rules. Lastly, Section 4.5 states formal properties of our algorithm.

4.1 Structure of the Search Space

The hypothesis space \mathcal{H} consists of a finite set of Datalog programs over the same input and output relations. For our running example (Example 2.3), we consider a simple hypothesis space where all programs use a subset of the following four rules:

$$\begin{aligned} r_1 &: \text{path}(x, y) :- \text{edge}(x, y). \\ r_2 &: \text{path}(x, z) :- \text{path}(y, z). \\ r_3 &: \text{path}(x, x) :- \text{edge}(x, x). \\ r_4 &: \text{path}(x, y) :- \text{path}(x, z), \text{path}(z, y). \end{aligned}$$

Algorithm 1 The ALPS synthesis algorithm

```

1:  $(E^+, E^-) \leftarrow (\emptyset, \emptyset)$ 
2:  $\bar{\mathbf{P}} \leftarrow \text{MostGeneral}()$ 
3:  $\underline{\mathbf{P}} \leftarrow \text{MostSpecific}()$ 
4: loop
5:    $\mathbf{P} \leftarrow \bar{\mathbf{P}} \cup \underline{\mathbf{P}}$  // construct committee
6:   if  $\forall e \in \mathcal{B}. D(e, \mathbf{P}) = 0$  then return  $\mathbf{P}$ 
7:    $e^* \leftarrow \operatorname{argmax}_{e \in \mathcal{B}} D(e, \mathbf{P})$  // most controversial example
8:    $\diamond \leftarrow O(e^*)$  //  $\diamond \in \{+, -\}$ 
9:    $E^\circ \leftarrow E^\circ \cup \{e^*\}$ 
10:   $\bar{\mathbf{P}} \leftarrow F^\downarrow(\bar{\mathbf{P}}, E^+, E^-)$  // top-down refinement
11:   $\underline{\mathbf{P}} \leftarrow F^\uparrow(\underline{\mathbf{P}}, E^+, E^-)$  // bottom-up refinement
12: end loop

```

We denote the Datalog program consisting of rules r_i, r_j, r_k as P_{ijk} .

Generality order. We structure the search by imposing a generality order on the space of Datalog programs. To define this order, we use θ -subsumption [54], which is a syntactic approach for deciding whether one rule subsumes (is more general than) another rule.

Formally, a rule C subsumes another rule D iff there is a variable substitution θ such that $C\theta$ has the same head as D , and all atoms in the body of $C\theta$ appear in the body of D .⁴ For example, r_2 subsumes r_4 with $\theta = \{z/y, y/z\}$, and r_1 subsumes r_3 with $\theta = \{y/x\}$.

Subsumption can be naturally extended from rules to programs. For any two Datalog programs P and Q , P subsumes Q , denoted $Q \sqsubseteq P$, iff for every rule in Q there exists a rule in P that subsumes it. For instance, in our running example, P_{13} subsumes P_{24} .

Given the hypothesis space \mathcal{H} , and a generality ordering \sqsubseteq , every subset \mathbf{P} of \mathcal{H} forms a quasi-ordered set w.r.t. \sqsubseteq . We can now construct a partial order on the quotient set of the equivalence relation (two programs P, Q are equivalent if $P \sqsubseteq Q$ and $Q \sqsubseteq P$).

In our running example, the following equivalence classes are formed w.r.t. θ -subsumption: $\{P_{1234}, P_{123}, P_{124}, P_{12}\}$, $\{P_{143}, P_{14}\}$, $\{P_{13}, P_1\}$, $\{P_{324}, P_{32}\}$, $\{P_{24}, P_2\}$, $\{P_{34}\}$, $\{P_3\}$, and $\{P_4\}$. We restrict the hypothesis space such that it has one representative from each class (any of the programs with the fewest rules) and define a partial order directly on these representatives instead of the equivalence classes. We can achieve this without any loss of generality since we are discarding only semantically equivalent programs. For our running example, the hypothesis space can now be reformulated as $\{P_{12}, P_{14}, P_1, P_{32}, P_2, P_{34}, P_3, P_4\}$.

Since the generality order is a partial order, there may exist multiple maximal and minimal elements. The set of maximal elements is denoted $\max(\mathbf{P}) = \{P \in \mathbf{P} \mid \nexists P' \in \mathbf{P}. P \sqsubset P'\}$, and we call these the *most-general* programs. Similarly, the set of minimal elements is denoted $\min(\mathbf{P}) = \{P \in \mathbf{P} \mid \nexists P' \in \mathbf{P}. P' \sqsubset P\}$, and we call these the *most-specific* programs. Figure 1a shows the initial version space for our running example, where the most-specific and most-general programs are colored yellow and red, respectively.

4.2 The ALPS Algorithm

Given a synthesis problem $S = (\mathcal{H}, O, I)$, ALPS applies Algorithm 1 to find a solution for S . It is a *fixpoint* algorithm that maintains a

⁴A substitution θ is a set $\{v_1/t_1, \dots, v_n/t_n\}$ where the v_i are distinct variables and t_i are terms. Notation $C\theta$ denotes the rule obtained by applying substitution θ on rule C , i.e., for each $v_i/t_i \in \theta$, we replace each occurrence of v_i in C by t_i .

pair $E = (E^+, E^-)$ of positive and negative examples, and a set of most-general programs $\bar{\mathbf{P}}$ and most-specific programs $\underline{\mathbf{P}}$ that are always consistent with E . The examples are initially empty, and $\bar{\mathbf{P}}, \underline{\mathbf{P}}$ are initialized to be the most general and most specific programs respectively (we define this initialization in Section 4.3). At every iteration, it adds a (positive or negative) example by querying the oracle O . Then, it invokes two refinement operators F^\uparrow, F^\downarrow which recalculate the most-general programs and the most-specific programs that agree with the new example (we define the refinement operators in Section 4.3). The algorithm stops when no new examples can be added.

The crux of the algorithm is the way we choose the example to query the oracle. The union of two sets of programs $\bar{\mathbf{P}}, \underline{\mathbf{P}}$ forms the *committee* \mathbf{P} . The committee then picks the most controversial example e^* . If $O(e^*) = +$, then e^* is added to E^+ ; otherwise, e^* is added to E^- . If no controversial example exists, then everyone in the committee agrees; the algorithm terminates and returns set \mathbf{P} , which contains all the most-general and most-specific solutions.

In order to determine the most controversial example, we use the metric of *vote entropy*. It is inspired by query-by-committee [24, 62], a greedy yet effective strategy commonly used in active learning [61]. Since there are only two possible labels for an example, we use a simplified definition, which is essentially equivalent to disagreement count.

Definition 4.1 (Vote entropy). For an example e and set of committee members K , the *normalized vote entropy* is:

$$D(e, K) = 1 - \frac{2}{|K|} \left| p - \frac{|K|}{2} \right|$$

where p is the number of committee members that assign a positive label to the example e .

When the vote entropy of an example is zero, all programs in the committee agree on its label. Figure 1 shows the version space and the query posed in each iteration for our running example.

4.3 Refinement with Meta-Rules

We now give concrete definitions of the initialization functions and refinement operators, F^\uparrow and F^\downarrow in Algorithm 1. The design of the refinement operators is motivated by a practical insight: the synthesis search should be biased towards patterns that are frequently used in practice. We are inspired by *meta-rules* [50], which are templates that dictate syntactic restrictions on rules and therefore a natural representation to bias the search.

Meta-rules. A *meta-rule* is a *second-order rule*. Multiple rules can be instantiated from a meta-rule. We shall use V_1 and V_2 to denote first- and second-order variables, respectively. A meta-rule takes the following form:

$$R_1(x_1, \dots, x_{m_1}) :- R_2(y_1, \dots, y_{m_2}), \dots, R_n(z_1, \dots, z_{m_n}).$$

where $x_i, y_i, z_i \in V_1$ and $R_i \in V_2$.

A meta-rule can be instantiated by substituting second-order variables with relation symbols. For example, the rules from the running example are generated by the following meta-rules:

$$\begin{aligned} T_1 &: R_0(x, y) :- R_1(x, y). \\ T_2 &: R_0(x, z) :- R_0(y, z). \end{aligned}$$

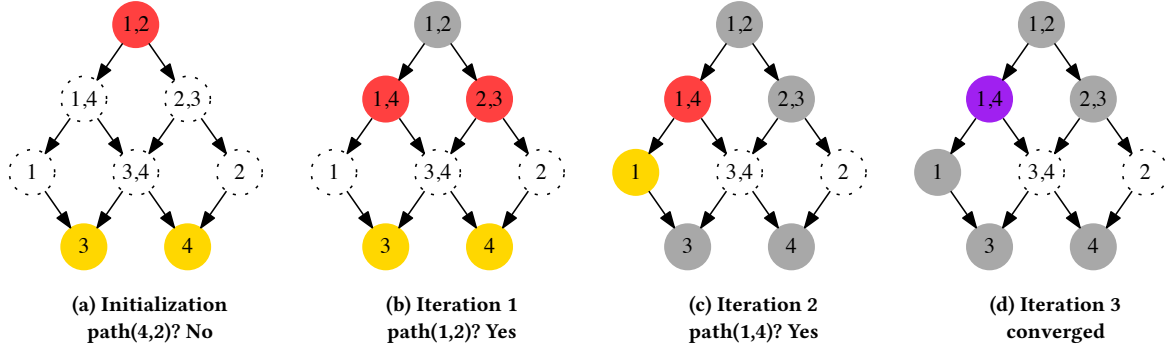


Figure 1: Version space in each iteration (red/yellow nodes represent most-general/specific programs in the current iteration; purple nodes represent programs that are both most general and most specific in the current iteration; and grey nodes represent programs that have been evaluated). An arrow from u to v means that program u is more general than program v .

Algorithm 2 Meta-rule-guided refinement

Function $F^\downarrow(\bar{P}, E^+, E^-)$	Function $F^\uparrow(\underline{P}, E^+, E^-)$
1: $E \leftarrow (E^+, E^-)$	1: $E \leftarrow (E^+, E^-)$
2: while $\bar{P} \not\subseteq \mathcal{V}_E$ do	2: while $\underline{P} \not\subseteq \mathcal{V}_E$ do
3: $\Delta\bar{P} \leftarrow (\bar{P} \cap \mathcal{V}_{E^+}) \setminus \mathcal{V}_{E^-}$	3: $\Delta\underline{P} \leftarrow (\underline{P} \cap \mathcal{V}_{E^-}) \setminus \mathcal{V}_{E^+}$
4: $\Delta\bar{P} \leftarrow \rho^\downarrow(\Delta\bar{P}, T) \cap \mathcal{V}_{E^+}$	4: $\Delta\underline{P} \leftarrow \rho^\uparrow(\Delta\underline{P}, T) \cap \mathcal{V}_{E^-}$
5: $\bar{P} \leftarrow (\bar{P} \cap \mathcal{V}_E) \cup \Delta\bar{P}$	5: $\underline{P} \leftarrow (\underline{P} \cap \mathcal{V}_E) \cup \Delta\underline{P}$
6: end while	6: end while
7: return \bar{P}	7: return \underline{P}

$$T_3 : R_0(x, x) :- R_1(x, x).$$

$$T_4 : R_0(x, z) :- R_0(x, y), R_0(y, z).$$

Similar to rules, a generality order between meta-rules can be established using θ -subsumption by allowing substitution for second-order variables as well as first-order variables. Using this generality order, a set of meta-rules forms a partially ordered set.

Initialization. The initialization function *MostGeneral()* collects all rules instantiated from the most general meta-rules and combines them as the most general program. The initialization function *MostSpecific()* makes each individual rule instantiated from the most specific meta-rules as a single rule program, and all of these programs form the initial set of most specific programs.

Meta-rule-guided refinement. Algorithm 2 describes our refinement operations, F^\downarrow and F^\uparrow , which are parameterized by a set of meta-rules T . We explain only top-down refinement F^\downarrow in detail, since bottom-up refinement F^\uparrow works in a symmetrical manner.

The algorithm begins with the given set of programs \bar{P} . Then, it iteratively *specializes* the programs by applying the specialization operator ρ^\downarrow , which is guided by T (line 2–5). In each iteration, the condition $\bar{P} \not\subseteq \mathcal{V}_E$ checks whether the current programs are consistent with the examples. If there is no violation, the algorithm terminates. Otherwise, line 3 first eliminates programs violating positive examples, and then selects programs violating negative examples to specialize. In the former case, programs fail to derive a positive example, and more specific programs will also fail to derive it. This process removes not only inconsistent programs but also any programs more specific than them. The elimination happens in the third iteration of our running example shown in Figure 1c:

when P_{23} is eliminated due to the positive example path(1,2), all the more specific programs P_{34}, P_2, P_3, P_4 are eliminated from consideration as well.

Next, line 4 specializes programs violating negative examples by calling ρ^\downarrow , and eliminates any generated programs that fail to derive a positive example. Finally, line 5 updates \bar{P} by including the new specialized programs.

The final piece of the puzzle is the *specialization operator* ρ^\downarrow . Here, ρ^\downarrow can specialize a program in two ways: (1) replace a rule it with a more specific one; for instance, in our running example shown in Figure 1b, program P_{12} is specialized to P_{14} and P_{23} ; (2) remove a rule that cannot be further specialized; for instance, P_{23} could potentially be specialized to P_2 . Finding all more specific rules for a given rule r can be efficiently done by consulting the generality order of the meta-rules T : first, find the meta-rule T_r used to instantiate r ; then, find all more specific meta-rules T_s with respect to T_r ; finally examine all rules instantiated from a meta-rule in T_s and keep the ones more specific than r .

4.4 Augmentation and Predicate Invention

The choice of meta-rules dictates the effectiveness of our synthesis algorithm. If the set of meta-rules is too large, then ALPS will not be able to scale, since the search space will be huge. On the other hand, the meta-rules must be sufficiently rich to capture the desired program. Simply reusing meta-rules that are either provided by the end-user or mined from existing code repositories is usually insufficient. To solve this problem, we start with a very small set of intuitive meta-rules that are specified manually (e.g., the chain meta-rule), and then extend these using *augmentation*, a process that slightly modifies each meta-rule.

An augmentation T' of a meta-rule T is a meta-rule where each atom $R(x_1, \dots, x_k)$ in T is replaced by another atom $R(y_1, \dots, y_\ell)$. However, we must take care to limit how much the sequence of variables changes. Denote by $d_R(T, T')$ the *edit distance* between the strings $x_1 \dots x_k$ and $y_1 \dots y_\ell$. Then, the *augmentation distance* between T, T' is defined as

$$AD(T, T') = \sum_R d_R(T, T')$$

where R ranges over all atoms in T . Our key idea is to consider all the augmentations of T that are within a bounded augmentation distance from T . The smaller this bound, the fewer meta-rules will be generated from T .

As an example of augmentation, consider these two meta-rules:

$$\begin{aligned} T_1 &: R_0(y) :- R_1(z), R_2(y, z). \\ T_2 &: R_0(y, z) :- R_1(z, x), R_2(y, z). \end{aligned}$$

Then, T_2 is an augmentation of T_1 with distance 2.

The augmentation distance required for ALPS to synthesize a program P from an initial set of meta-rules T is:

$$AD(P, T) = \max_{T_1} \min_{T_2 \in T} AD(T_1, T_2)$$

where T_1 ranges over all meta-rules used in P_1 . In our experiments, we could synthesize almost all of the programs using an augmentation distance of 5 from three chain meta-rules.

Predicate invention. Another orthogonal way to improve the richness of programs in the search space is predicate invention. Predicate invention helps to break a complex rule into simpler ones, and thereby enables to reuse existing meta-rules. More importantly, it is unavoidable for Datalog programs with recursion. For instance, consider the following program which computes strongly connected components (SCC) in a directed graph:

$$\begin{aligned} \text{path}(x, y) &:- \text{edge}(x, y). \\ \text{path}(x, z) &:- \text{path}(x, y), \text{edge}(y, z). \\ \text{scc}(x, y) &:- \text{path}(x, y), \text{path}(y, x). \end{aligned}$$

Here, the input and output relations are `edge` and `scc`, respectively. Given that `scc` cannot be derived by any set of clauses in terms of only the input relation `edge`, a new predicate `path` must be invented. The difficulty with predicate invention lies in determining what form the invented predicates should take. Without meta-rules, we have no way to effectively constrain the syntax of such predicates. With meta-rules, we can easily support predicate invention: the rules that define the potential invented predicates are exactly the instantiations of meta-rules with concrete relations.

4.5 Properties of ALPS

The ALPS synthesis algorithm (Algorithm 1) always makes progress: after every query to oracle O , we remove from consideration a controversial example from \mathcal{B} . Since the set of possible examples \mathcal{B} is finite, the algorithm always terminates. It also guarantees that a solution is found if there are no controversial examples left in the committee. To ensure this property, it is critical that the algorithm tracks both the most-general and most-specific programs at every iteration. The following theorem succinctly captures these properties. We provide its proof in the Appendix.

THEOREM 4.2. *Let $S = (\mathcal{H}, O, I)$ be a synthesis problem such that a solution to S exists in \mathcal{H} . Let \mathbf{P} be the output of ALPS. Then:*

- (1) (Soundness) Every $P \in \mathbf{P}$ is a solution to S .
- (2) (Completeness) For every solution $P \in \mathcal{H}$ to S , there exist programs $P_l, P_u \in \mathbf{P}$ such that $P_l \sqsubseteq P \sqsubseteq P_u$. An immediate corollary is that if there exists a program P that is a solution to S , then \mathbf{P} is nonempty.
- (3) (Termination) ALPS terminates in finitely many steps.

5 EMPIRICAL EVALUATION

We evaluate ALPS on a variety of synthesis tasks from different domains. Our implementation⁵ comprises about 8,000 lines of C++ code. It uses the fixpoint engine of the Z3 SMT solver [31] for Datalog evaluation. Our experiments were performed on a Linux machine with 16 GB of RAM and a 3.0 GHz processor.

Our evaluation aims to answer the following questions:

- Q1. How does ALPS perform on synthesis tasks from a variety of domains in terms of synthesis time and number of queries?
- Q2. How much does meta-rule augmentation speed up synthesis?
- Q3. How effective is QBC in reducing the number of queries asked?
- Q4. How sensitive is ALPS to changes in a given input data?
- Q5. How does ALPS compare with existing synthesis techniques?

5.1 Benchmark Suite

We collected 34 synthesis tasks from three different application domains: (i) knowledge discovery, (ii) program analysis and (iii) relational queries. Table 1 presents useful characteristics of these benchmarks. The last three columns show the number of input-output relations, the number of rules of the smallest desired program, and whether the desired program is recursive or not, respectively.

Knowledge discovery. The knowledge discovery benchmarks comprise 8 tasks of synthesizing Datalog programs frequently used in the artificial intelligence and database literature. The goal of the first benchmark `inflammation` is to discover interesting correlations between patient risk factors and a disease called acute inflammations of urinary bladder. We used a dataset created by a medical expert to enable expert systems that perform presumptive diagnosis of the disease [20].⁶ The next four benchmarks (`abduce`, `ancestor`, `animals`, and `buildWall`) are widely used in the field of inductive logic programming [46, 50]. The `samegen` benchmark is a standard Datalog program in the database literature [7]. The `path` benchmark is the problem described in Example 2.3 and the `scc` benchmark is the problem of computing strongly connected components in a directed graph.

Program analysis. The program analysis benchmarks comprise 11 tasks of synthesizing static analyzers written in Datalog:

- `polysite` is a polymorphic call-site inference analysis for Java;
- `downcast` is a downcast safety checker for Java;
- `rv-check` is the static API misuse detector described in Example 2.1, which is motivated from a return value checker used in a tool called `APISAN` [72]. `APISAN` identifies API misuses by detecting inconsistent uses of the return values of API functions. However, the tool is neither sound nor complete due to the limitation of its statistical method. This observation motivated our rule-based approach for static API misuse detection.
- `andersen` is a classic pointer analysis for C [12];
- The next five benchmarks are pointer analyses for Java with various context abstractions [42, 66, 70].
- `modref` is a mod-ref analysis for Java and `escape` is an escape analysis for Java. Both benchmarks originated from a programming assignment in an online course on program analysis [5].

⁵Our artifact is available on GitHub: <https://github.com/XujieSi/fse18-artifact-183>.

⁶Available at <http://archive.ics.uci.edu/ml/datasets/Acute+Inflammations>.

Table 1: Benchmark characteristics.

Benchmark	Brief description	#Relations	#Rules	Recursive?
<i>Knowledge Discovery</i>				
inflammation	diagnosis of bladder inflammation	7	2	
abduce	grandparent of given father/mother [46]	4	3	
animals	distinguishing classes of animals [46]	13	4	
ancestor	ancestor in a family tree [50]	4	4	✓
buildWall	learn a stable wall strategy [50]	5	4	✓
samegen	same generation in a family tree [7]	3	3	✓
path	all-pairs reachability in directed graph	2	2	✓
scc	compute SCCs in directed graph	3	3	✓
<i>Program Analysis</i>				
polysite	polymorphic call-site inference for Java	6	3	
downcast	downcast safety checker for Java	9	4	
rv-check	return-value-checker in APISan [72]	5	5	
andersen	inclusion-based pointer analysis for C [12]	5	4	✓
1-call-site	1-call-site pointer analysis for Java [70]	9	4	✓
2-call-site	2-call-site pointer analysis for java [70]	9	4	✓
1-object	1-object-sensitive pointer analysis [42]	11	4	✓
1-type	1-type-sensitive pointer analysis [66]	12	4	✓
1-obj-type	1-type-1-object sensitive analysis [66]	13	5	✓
escape	escape analysis for Java	10	6	✓
modref	mod-ref analysis for Java	13	10	✓
<i>Relational Queries</i>				
sql-1 ~ 15	15 SQL queries [69]	≤ 7	≤ 4	

Relational queries. These benchmarks comprise 15 synthesis tasks from Stack Overflow posts and textbook examples [69]. We chose the 15 tasks of synthesizing SQL queries that can be expressed in Datalog. Each task involves up to 6 input tables and one output table. The desired Datalog programs comprise up to four rules.

5.2 Experimental Setup

Meta-rules. We first apply only the following three chain meta-rules with up to 5 augmentations for all benchmarks:

$$\begin{aligned}
 R_0(v_1, v_2) & :- R_1(v_1, v_2). \\
 R_0(v_1, v_3) & :- R_1(v_1, v_2), R_2(v_2, v_3). \\
 R_0(v_1, v_4) & :- R_1(v_1, v_2), R_2(v_2, v_3), R_3(v_3, v_4).
 \end{aligned}$$

We observe that ALPS fails to synthesize five context-sensitive pointer analysis benchmarks, as the necessary augmentation distance is too far and offers no filtering of the search space. In these cases, we also include domain specific meta-rules, e.g. meta-rules extracted the remaining four benchmarks. Also, we set the maximum number of invented predicates to 4.

Input-output relations. For each benchmark, ALPS begins with no examples of output relations and iteratively poses membership queries about the contents of the output relations. To answer such queries, we used the known solution of the benchmark (i.e., the desired Datalog program) as an oracle. The populated input relations range in size from 3 to 77 with an average of 22.

5.3 Evaluation Results

Q1: Number of queries and synthesis time. Table 2 presents the main results of our evaluation. Consider, for instance, the ancestor benchmark. ALPS makes 11 queries to the oracle (out of a maximum of 450 queries, which is the size of the Herbrand base); it takes 25

seconds to synthesize 3 programs; and, in the process, it evaluates 24,280 programs out of 10^{10} programs in the search space.

Overall, our results demonstrate the small number of queries needed to discover non-trivial programs. For most benchmarks, ALPS requires less than 20 queries; for our largest benchmark, mod-ref, ALPS makes 22 queries to the oracle in order to synthesize 10 rules. It synthesizes most programs within a few minutes. In certain examples—like mod-ref—a large number of programs are evaluated, thus requiring more synthesis time.

Q2: Effectiveness of meta-rule augmentations. Figure 3 shows the frequency distribution of benchmarks according to their augmentation distance with respect to chain meta-rules. Only two benchmarks can be synthesized with no augmentation, while most benchmarks (29 out of 34) can be synthesized with no more than 5 augmentations. This indicates that simple chain meta-rules are quite limited by themselves, but we can handle a large number of benchmarks by slightly mutating them.

Starting with only chain meta-rules, however, ALPS fails to scale on five context-sensitive pointer analysis benchmarks, whose augmentation distance is 6 or larger. We observe that although these five benchmarks are different from each other, their rules are quite similar. Table 3 shows the augmentation distances for each of these five benchmarks with respect to two sets of meta-rules: chain meta-rules and meta-rules mined from the other four benchmarks. The augmentation distance implies that, in comparison with general chain meta-rules, meta-rules mined from the same domain are more useful to guide the synthesis search process. Indeed, with extra meta-rules mined from the other four benchmarks, ALPS is able to synthesize four of the five context-sensitive pointer analysis benchmarks, as shown in Table 2.⁷

Q3: Quality of QBC. We now investigate the quality of QBC’s selection strategy. To do so, we instrument ALPS to randomly pick an example that the committee disagrees on, instead of one that maximizes vote entropy. For each benchmark⁸, we ran 100 trials with random example selection. Figure (2a) shows a box plot of the number of queries made in these trials. We see that random selection, on average, performs much worse than QBC. For instance, on the ancestor benchmark, the median for random selection is more than 120 queries, while QBC only needs 11.

Compared to the best-case scenarios of random selection, QBC makes roughly the same amount (about +/-5 queries) of queries for most benchmarks. For the andersen benchmark, one random trial behaves surprisingly well: it only requires 8 questions to synthesize all 4 expected rules, one of which eliminates 99.7% of the committee members. This is an artifact of QBC’s *conservative* example-selection approach: it prefers high-entropy examples, so it may miss a low-entropy example that could eliminate most of the committee, indicating QBC is not optimal but practically effective.

Q4: Sensitivity to the size of input data. We now investigate the effects of increasing the size of input data on the number of queries needed. We focus on the andersen benchmark, as it is demonstrative of the behavior across our benchmark suite. Recall

⁷1-obj-type takes ALPS 17 hours to finish and hence is marked as timeout.

⁸We skip the SQL benchmarks as ALPS asks a very small number of queries for them.

Table 2: ALPS performance results (the timeout limit is 3 hours).

	#queries asked by ALPS	#possible queries	#synthesized programs	#evaluated programs	search space	total time (sec.)	Metagol run. time (sec.)		Zaatar run. time (sec.)
							ALPS setting	ideal setting	
inflammation	8	120	4	2327	10^6	4.3	0.51	0.47	timeout
abduce	11	392	1	4613	10^6	3.36	timeout	0.43	timeout
animals	16	80	2	45152	10^6	75.8	0.46	0.42	timeout
ancestor	11	450	3	24280	10^{10}	24.6	timeout	0.43	timeout
buildWall	12	392	13	61654	10^{10}	128.7	timeout	35.1	timeout
samegen	12	162	2	110338	10^9	22.3	timeout	timeout	4.77
path	4	49	3	384	10^4	0.26	timeout	0.43	26.43
scc	14	128	4	57013	10^6	88.7	timeout	timeout	timeout
<hr/>									
polysite	14	204	5	27432	10^{22}	130.0	timeout	0.43	timeout
downcast	9	912	1	56489	10^{28}	299.8	timeout	0.43	timeout
rv-check	4	24	1	393740	10^{29}	361.5	timeout	timeout	timeout
andersen	15	64	1	100345	10^{20}	148.0	timeout	timeout	295.31
1-call-site	14	152	3	99697	10^{32}	178.3	timeout	timeout	timeout
2-call-site	17	672	1	184824	10^{53}	601.8	timeout	timeout	timeout
1-object	18	655	1	93362	10^{48}	705.1	timeout	timeout	timeout
1-type	13	215	2	10038	10^{30}	21.6	timeout	timeout	timeout
1-obj-type	-	-	-	-	10^{51}	timeout	timeout	timeout	timeout
escape	9	40	12	5706	10^{34}	9.9	timeout	timeout	timeout
modref	22	145	1	1346754	10^{45}	5307	timeout	timeout	timeout
<hr/>									
sql-1	4	7	1	30	10^6	0.07	0.01	0.01	43.65
sql-2	3	12	1	7	10^6	0.02	0.01	0.01	timeout
sql-3	1	4	1	1	10^1	0.03	0.01	0.01	timeout
sql-4	5	15	1	19	10^2	0.02	0.01	0.01	timeout
sql-5	1	7	1	1	10^2	0.01	0.01	0.01	timeout
sql-6	6	729	1	44	10^2	0.03	0.01	0.01	timeout
sql-7	1	25	1	1	10^1	0.01	0.01	0.01	timeout
sql-8	5	48	2	230	10^{16}	1.60	0.02	0.01	timeout
sql-9	5	27	1	9	10^{16}	0.30	timeout	0.01	6260
sql-10	8	40	1	778	10^{23}	63.2	timeout	0.01	timeout
sql-11	4	25	6	1192	10^{18}	1.86	timeout	0.04	8320
sql-12	4	34	1	117	10^{15}	0.20	timeout	timeout	2417
sql-13	3	80	1	4	10^3	0.01	timeout	timeout	timeout
sql-14	3	651	1	13	10^{25}	90.9	timeout	timeout	timeout
sql-15	5	266	1	344	10^{15}	17.7	timeout	timeout	timeout

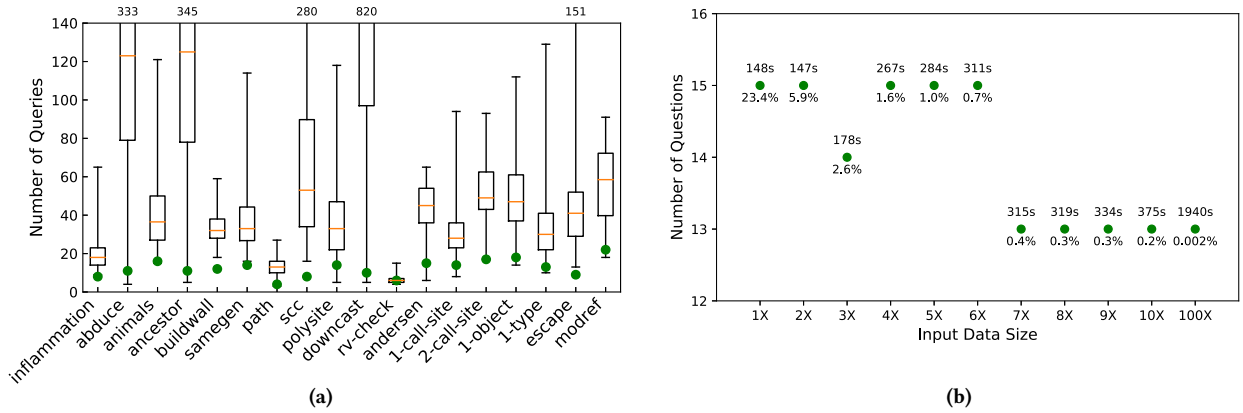


Figure 2: (a) Box plot of the number of queries asked by random selection (green dots mark the number of queries by QBC); and (b) Number of queries asked by ALPS for the andersen benchmark under different sizes of input data (where X=7).

that andersen is a pointer analysis for C programs. We systematically increased the size of the input data (i.e., the size of the analyzed program), and measured the number of queries needed to synthesize Andersen’s analysis, as well as the synthesis time. Figure (2b) summarizes the results of this experiment. It shows that as the size of the data increases, the number of questions asked stays roughly constant. As a result, the question ratio (number of questions asked to the total number of possible questions) is reduced

significantly, from nearly 25% to 0.002%. The number of evaluated programs also remains roughly constant. As expected, the synthesis time increases with more data, as ALPS needs to invoke the Datalog solver on larger inputs.

Q5: Comparison with other tools. We now compare ALPS with two state-of-the-art ILP tools: Metagol [19] and Zaatar [9]. We

Table 3: Augmentation distances of context-sensitive pointer analysis benchmarks with respect to chain meta-rules and meta-rules mined from the same domain.

	1-call-site	2-call-site	1-object	1-type	1-obj-type
chain	6	8	6	6	8
same domain	3	3	1	2	2

supply both of these tools with all ground facts upfront since they are non-interactive.

Metagol is an ILP tool that is an instance of the *meta-interpretive learning* framework [50], which is also parameterized by meta-rules. We run Metagol with two settings: the ALPS setting, which uses the same set of meta-rules that ALPS uses after it performs augmentation, and the ideal setting, which consists of the minimal set of meta-rules that are sufficient for synthesizing a correct program. Using ALPS's setting, Metagol cannot finish most knowledge discovery benchmarks and all program analysis benchmarks. Using the ideal setting, Metagol still fails on two knowledge discovery benchmarks and most of program analysis benchmarks. Metagol also fails on four of the SQL benchmarks despite their lack of recursion. It is important to note that Metagol employs meta-interpretive learning, which is not a complete technique, so it is not guaranteed to terminate, despite finiteness of the search space.

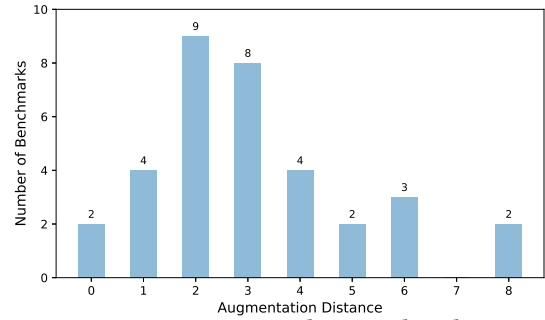
Zaatar [9] is a constraint-based Datalog program synthesis tool. It fails on most of our benchmarks because it is very sensitive to the size of the input data, since the size of the encoding is polynomial in the input data. In contrast, ALPS has much better scalability in terms of input size, as ALPS only evaluates candidate programs on input data instead of encoding the input as symbolic constraints.

Summary. To summarize, our experimental evaluation demonstrates (i) the ability of ALPS to synthesize sophisticated algorithms; (ii) the effectiveness of meta-rules and augmentations; (iii) the importance of QBC at reducing the number of queries; and (iv) the robustness of our synthesis approach to input size.

5.4 Threats to Validity

There are several threats to the validity of our approach. We outline these next along with proposals to mitigate them.

- ALPS may fail to synthesize a desirable program because the input relations do not cover all corner cases (i.e., overfitting). We can mitigate this threat by allowing the user to provide a large input and taking advantage of ALPS's ability to handle sizeable input data as shown in Figure (2b). In practice, large input relations often cover the vast majority of corner cases.
- The labeled examples may be noisy. This threat can be mitigated by collecting answers from multiple oracles (e.g., through crowdsourcing or multiple reference implementations) and using the majority vote as the final answer.
- A large number of equivalent final programs exist due to many applicable combinations of meta-rules. This threat can be mitigated by sacrificing completeness and reporting a subset of programs.
- The meta-rules generated by ALPS may be insufficient to capture a desired program. This threat can be mitigated by using a larger number of invented predicates. The more such predicates we use, the simpler rules we obtain. Eventually, the desired program will comprise typical rules, thus enabling ALPS to synthesize it.

**Figure 3: Augmentation distance distribution.**

6 RELATED WORK

Inductive logic programming. While we use key ideas from inductive logic programming (ILP) in ALPS, a number of properties distinguish our approach from existing ILP approaches. First, work in ILP usually learn relations, often probabilistic ones [21], from vast amounts of mined data, e.g., biological data [47]. In our work, and in a large class of synthesis techniques, the goal is to *interactively* infer a program from a *small, representative set of examples*. Second, most ILP systems are not adept at learning recursive rules. In contrast, we specifically aim to infer recursive rules. Third, ILP is often interested in programs that correctly classify *most* examples. In contrast, we are interested in programs that correctly characterize *all* positive and negative examples. Fourth, many ILP systems require a complicated interaction model (for example, FILP [15] poses existential queries and CIGOL [48] poses generalization queries). In contrast, ALPS has a simple interaction model that only poses membership queries. Lastly, we employ a *complete* search strategy, whereas ILP systems can fail to find a program even if one exists that is consistent with the given examples.

More recently, ILP has been applied to end-user programming and online tutoring [29]. Meta-Interpretive Learning has been used to learn Prolog programs for string manipulation tasks [38]. These applications share similar goals as ours of learning programs by obtaining examples from users. We focus on Datalog programs whereas they learn programs in other domains, e.g., string manipulation or table transformation. Also, when their generated program is incorrect, the user is expected to provide a counterexample. In contrast, our approach automatically identifies the most controversial example to pose to the user.

Template-guided synthesis. Templates are commonly used to guide the search in program synthesis [19, 64, 67, 68]. At a high-level, meta-rules can also be seen as program sketches [67], where the holes are the relation symbols.

Interactive synthesis by example. Some of the programming-by-example (PBE) approaches interactively query an oracle for examples. Jha et al. [32] present an oracle-guided synthesis procedure for straight-lines programs encodable in smt. They require the oracle (usually a reference implementation) to provide the output when given some input. Another recent interactive synthesis approach is applied in the context of parser synthesis [37] to learn a grammar.

Synthesis of recursive programs. A number of works have targeted the problem of synthesizing recursive programs [8, 23, 34, 35,

53, 55]. Most of these works focus on recursive functional programs that manipulate recursive data structures. Datalog programs recursively traverse relations (hypergraphs). To our knowledge, none of the functional techniques have been applied to this domain.

Version-space algebras. Version-space algebras were used for synthesis, initially by Lau et al. [36], and more recently in Flash-Fill [28] for spreadsheet manipulation. ALPS maintains a version space using most-general and most-specific programs, as first proposed by Mitchell [43]. Our setting is different than Mitchell’s in the sense that the search space is determined by a set of meta-rules that forms a partially ordered set, and thereby we can exploit the generality order on the meta-rules for our bidirectional search.

Learning for program analysis. Recently, several systems have been created that apply machine learning techniques to program analysis. Oh et al. [52] use Bayesian optimization techniques to effectively learn adaptation strategies for parametric program analysis, while Bielik et al. [16] apply the ID3 algorithm to learn a decision tree that represents points-to and allocation site facts for individual JavaScript functions. This work either learns an efficient configuration for program analysis or an accurate representation for the results of an analysis. In contrast, our work can learn the rules of the program analysis, expressed in Datalog.

7 CONCLUSIONS AND FUTURE WORK

We proposed a programming-by-example system, ALPS, to synthesize Datalog programs. It employs a syntax-guided synthesis approach that prunes the search space by exploiting the observation that Datalog programs in practice comprise rules with similar latent syntactic structure. To this end, we synergistically combined three techniques: a novel approach to systematically generate meta-rules, taking advantage of domain knowledge; an active learning technique called query-by-committee to minimize the number of examples needed; and a bidirectional synthesis strategy to explore the search space efficiently. We evaluated the system on a variety of synthesis tasks from different domains and demonstrated that it significantly outperforms existing state-of-the-art tools.

We envision many useful directions to extend our work. One direction concerns repairing existing Datalog programs using examples rather than synthesizing them from scratch. For instance, a user may modify an existing program analysis by refining its rules to be consistent with known true and false positives. Another direction concerns using probabilistic models to expedite the search, for instance, by predicting which augmentations to use. Finally, we plan to explore how to synthesize programs that are not only correct with respect to examples, but also optimal with respect to objectives such as likelihood or evaluation complexity.

A PROOF OF ALPS PROPERTIES

To prove Theorem 4.2, we use two key properties about the interplay between QBC and bidirectional search. The following lemma captures the fact that the algorithm does not miss any controversial examples, and thus always makes progress in terms of pruning the search space.

LEMMA A.1. *Let $\mathbf{P} \subseteq \mathcal{H}$ and $e \in \mathcal{B}$. Then $D(e, \mathbf{P}) \neq 0$ iff there exist programs $P_1, P_2 \in \mathbf{P}$ such that $P_1 \cup I \models e$ and $P_2 \cup I \not\models e$.*

PROOF. This is directly implied by the definition of vote entropy (see Definition 4.1). ■

The next lemma states key invariants that hold at every iteration of the algorithm: (i) It does not miss any programs that are solutions to the synthesis problems, by ensuring that the contours of the version space form an upper/lower bound of every solution. (ii) It ensures that if the current version space contains non-solutions, then there are non-zero entropy examples we can ask the oracle that can eliminate them.

LEMMA A.2 (INVARIANT). *Let $S = (\mathcal{H}, O, I)$ be a synthesis problem such that a solution to S exists in \mathcal{H} . Let $E = (E^+, E^-)$ be the set of known examples at any point during execution, and $\mathbf{P} = \overline{\mathbf{P}} \cup \underline{\mathbf{P}}$. Then:*

- (1) *For every solution $P' \in \mathcal{H}$ to S , there exist programs $P_l, P_u \in \mathbf{P}$ such that $P_l \sqsubseteq P' \sqsubseteq P_u$.*
- (2) *If there exists a program $P \in \mathbf{P}$ that is not a solution to S , then $\exists e \in \mathcal{B}. D(e, \mathbf{P}) \neq 0$.*

PROOF. We first show item (1). First, notice that every solution $P' \in \mathcal{H}$ to S belongs in the version space \mathcal{V}_E , since it satisfies all current examples. Since $\mathbf{P} \supseteq \max(\mathcal{V}_E)$ (by the definition of F^\uparrow in Algo. 1), there exists $P_u \in \mathbf{P}$ such that $P' \sqsubseteq P_u$. Similarly, since $\mathbf{P} \supseteq \min(\mathcal{V}_E)$, there exists $P_l \in \mathbf{P}$ such that $P_l \sqsubseteq P'$.

We next show item (2). Suppose that $P \in \mathbf{P}$ is not a solution to S , and let P' be a solution to S . Then, there exists an example $e \in \mathcal{B}$ such that either (a) $P \cup I \models e$ and $P' \cup I \not\models e$, or (b) $P \cup I \not\models e$ and $P' \cup I \models e$. We now distinguish two different cases:

- Case (a) holds: since P' is a solution, item (1) tells us that there exists $P_u \in \mathbf{P}$ such that $P' \sqsubseteq P_u$. This implies that $P_u \cup I \not\models e$. Because now P, P_u disagree on example e , Lemma A.1 implies that $D(e, \mathbf{P}) \neq 0$.
- Case (b) holds: since P' is a solution, item (1) tells us that there exists $P_l \in \mathbf{P}$ such that $P_l \sqsubseteq P'$. This implies that $P_l \cup I \models e$. Because now P, P_l disagree on example e , Lemma A.1 implies that $D(e, \mathbf{P}) \neq 0$.

Thus, in both cases we find an example e such that $D(e, \mathbf{P}) \neq 0$. ■

We are ready to prove Theorem 4.2 using the Lemmas A.1 and A.2.

PROOF. The algorithm terminates when for every example $e \in \mathcal{B}$, we have $D(e, \mathbf{P}) = 0$. Recall that $\mathbf{P} = \overline{\mathbf{P}} \cup \underline{\mathbf{P}}$, where $E = (E^+, E^-)$ are the known examples.

- (Soundness) As $\forall e \in \mathcal{B}. D(e, \mathbf{P}) = 0$, the contrapositive of item (2) of Lemma A.2 indicates that every $P \in \mathbf{P}$ is a solution.
- (Completeness) This holds directly from item (1) of Lemma A.2.
- (Termination) At every iteration, the algorithm adds one example to either E^+ or E^- . Notice that, after an example e is added to $E = (E^+, E^-)$, it cannot be added again, since it will never be controversial ($D(e, \mathbf{P}) \neq 0$) from that point on. Since we have finitely many examples in \mathcal{B} , the algorithm terminates after finitely many steps.

This concludes the proof of the theorem. ■

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